

13. Bayes' Theory
$$p(F | E) = \frac{p(E | F) p(F)}{p(E | F) p(F) + p(E | \bar{F}) p(\bar{F})}$$

8% use steroids

96% test positive given use steroids

9% test positive given not use steroids

E = test positive.

F = use steroids.

$p(F) =$

$p(E|F) =$ test positive given use =

$p(E | \bar{F}) =$ test positive given not use =

$p(F|E) =$ use steroids given test positive =

14. Expected Value

Wins \$1000 if dealt 3 of a kind in poker, ignoring full house.

What is expected value of one hand?

$|K3|$ = 3 of a kind =

$|S|$ = # poker hands =

$p(K3)$ = probability of winning =

$E(K3)$ = expected value of winning

15. Expected number of heads in 2 flips?

$S = ?$

$X(s)$ is number of heads

$X(HH) = ?$

$X(HT) = ?$

$X(TH) = ?$

$X(TT) = ?$

$$E(X) = \sum_{s \in S} p(s)X(s)$$

$s \in S, X(s) = ?$

$\forall s \in S, p(s) = ?$

$E(X) = ?$

13.

Bayes' Theory

$$p(F | E) = \frac{p(E | F) p(F)}{p(E | F) p(F) + p(E | \bar{F}) p(\bar{F})}$$

8% use steroids

96% of users test positive

9% of non-users test positive

E = test positive.

F = use steroids.

$$p(F) = 8\%$$

$$p(E|F) = \text{test positive given user} = 96\%$$

$$p(E | \bar{F}) = \text{test positive given not user} = 9\%$$

$$\begin{aligned} p(F|E) &= \text{use steroids given test positive} \\ &= .96*.08 / (.96*.08 + .09*.92) \\ &= .481 \end{aligned}$$

14.

Expected Value

Wins \$1000 if dealt 3 of a kind in poker. Ignoring full-houses.

What is expected value of one hand?

$$|K3| = 3 \text{ of a kind} = C(13,1)*C(4,3)*C(48,2)$$

C(13,1) is the 1 of 13 kinds

C(4,3) is the 3 of 4 of one kind

C(48,2) is remaining two cards, excluding the 4 of a kind.

$$= 13*4*1128 = 58656$$

$$|S| = \text{poker hands} = C(52,5) = 2598960$$

$$p(K3) = \text{probability of winning} = 0.022569$$

E(K3) = expected value of winning

$$= p(K3)*X(K3) = 0.022569 * \$1000 = \$22.57$$

15. Expected number of heads in 2 flips?

$$E(X) = \sum_{s \in S} p(s)X(s)$$

$$S = \{HH, HT, TH, TT\}$$

$$X(HH) = 2$$

$$X(HT) = 1$$

$$X(TH) = 1$$

$$X(TT) = 0$$

$$s \in S, X(s) = \{2, 1, 1, 0\}, \forall s \in S, p(s) = \frac{1}{4}$$

$$E(X) = (2/4 + 1/4 + 1/4 + 0/4) = 4/4 = 1$$