

For positive integer n :

$$1^2 + 2^2 + 3^2 + \dots + n^2 = n(n+1)(2n+1)/6$$

1. What is the $n = 1$?
2. What is $n = 2$?
3. Hypothesis? $P(n) =$
4. Basis step? $P(1) =$
5. Inductive step? $P(k) =$
6. Must show? $P(k+1) =$

Add what to both sides of $P(k) =$.

Prove, using induction, that the sum of the first n even positive integers is:

$$2+4+6+\dots+2n = n(n+1)$$

7. What is the sum for $n=1$?

8. Hypothesis? $P(n) =$

9. Basis step? $P(1) =$

10. Inductive step? $P(k) =$

11. Must show? $P(k+1) =$

12. Proof

Hint: Add $2(k+1)$ to both sides of $P(k)=$

Prove that 2 divides n^2+n for positive integers:

13. Hypothesis? $P(n)$

14. Basis step? $P(1)$

15. Inductive step? $P(k)$

16. Must show? $P(k+1)$

17. Proof

Prove, using induction, for n positive integer:

$$1^2 + 2^2 + 3^2 + \dots + n^2 = n(n+1)(2n+1)/6$$

1. What is the $n = 1$? 1
 2. What is $n = 2$? 5
 3. Hypothesis? $P(n) = n(n+1)(2n+1)/6$
 4. Basis step? $P(1) = 1$
 5. Inductive step? $P(k) = k(k+1)(2k+1)/6$
 6. Must show? $P(k+1) = (k+1)(k+1+1)(2(k+1)+1)/6$
- Hint: Add $(k+1)^2$ to both sides of $P(k) =$

Prove, using induction, that the sum of the first n even positive integers is:

$$2+4+6+\dots+2n = n(n+1)$$

7. What is the sum for $n=1$. $2 = 1(1+1) = 2$

8. Hypothesis? $P(n) = 2+4+6+\dots+2n = n(n+1)$

9. Basis step? $P(1) = 1(1+1) = 2$

10. Inductive step? $P(k) = (2+4+6+\dots+2k) = k(k+1)$

11. Show? $P(k+1) = (2+4+6+\dots+2k) + 2(k+1)$
 $= (k+1)((k+1)+1) = (k+1)(k+2)$

12. Proof

$$P(k) = 2 + 4 + 6 + \dots + 2k$$

$$= k(k+1)$$

Inductive
Hypothesis

$$P(k+1) = \\ (2 + 4 + 6 + \dots + 2k) + 2(k+1)$$

$$= k(k+1) + 2(k+1)$$

Add $2(k+1)$ to
both sides of $P(k)$

$$= k^2 + k + 2k + 2$$

Multiply

$$= k^2 + 3k + 2$$

Add

$$= (k+1)(k+2)$$

Factor

Prove that 2 divides n^2+n for positive integers:

13. Hypothesis? $P(n)$ 2 divides n^2+n

14. Basis step? $P(1)$ 2 divides $1^2+1 = 2$

15. Inductive step? $P(k)$ 2 divides k^2+k

16. Must show? $P(k+1)$ 2 divides $(k+1)^2+(k+1)$

17. Proof

$$\begin{aligned}(k+1)^2+(k+1) &= k^2 + 2k + 1 + k + 1 \\ &= k^2 + k + 2(k+1)\end{aligned}$$

$P(k)$ 2 divides k^2+k

2 divides $2(k+1)$